Name: Solutions

Date: 5/6/2025

Math 130 Exam 4

Please show ALL your work on the problems below. No more than 1 point will be given to problems if you only provide the correct answer and insufficient work.

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Subject	1	2	3	4	5	6
Braking Time With Normal Vision (seconds)	4.4	4	5.3	5.7	4.8	4.1
Braking Time With Impaired Vision (seconds)	5.7	5.8	5.1	6.5	5.7	5.8
Dichelances (Impailed - Normal)	1.3	1.8	-0.2	0.8	0.9	1.7

Test the claim that braking time is longer with impaired vision than with normal vision at the 0.02 significance level. Use the rejection region method.

Hyp Test Ho: Md = O H1: Md >0 Md = The average of all differences in broching time (Impaired - Normal) time time

 $\frac{\text{Rejection Region}}{\alpha = 0.02} \quad dF = n - 1 = 6 - 1 = 5$



$$\frac{\text{Test 5tot}}{n:6}$$

$$\overline{d} = \frac{1.3 + 1.8 + \dots + 1.7}{6} = 1.05$$

$$\sum_{x}^{9} = 1.3^{2} + 1.8^{2} + \dots + 1.7^{2} = 9.31$$

$$\overline{\sum_{x}^{2} - 1.3 + 1.8 + \dots + 1.7} = 6.3$$

$$S_{d} = \sqrt{\frac{\sum_{x}^{2} - \frac{(\sum_{x})^{2}}{n}}{n-1}} = \sqrt{\frac{9.31 - (6.3)^{2}}{6-1}} = 0.7341661937$$

$$t = \frac{\overline{d} - Md}{\frac{54}{\sqrt{n}}} = \frac{1.05 - 0}{\frac{0.7341661937}{\sqrt{6}}} = (3.503245249)$$

Conclusion Reject Ho!

Evidence Guggests that braking time is longer (on average) with impaired vision than for normal vision.

1-pop average problem

2. (22 points) Some people have said that a college education is not as important as it once was. One way to test this is to look at how having a college degree effects a person's salary. As of today, the average salary of all people in California is \$73,220 per year. Do California employees with a college degree make the same? To test this, 100 California employees with a college degree were polled and their salaries had a mean of \$91,380 and a standard deviation of \$3920. Test this claim at the 0.10 significance level. Use the rejection region method.

Hyp. Test	Rejection Region
$H_{0}: \mu = $73,220$ $H_{1}: \mu \neq $73,220$	X=0,10 dF=n-1=100-1=99 (USe 100)
M= The average salary of all California employees that have a college degree	$\begin{array}{c} 0.05 \\ 0.$
$\frac{1}{100} = \frac{100}{100} = $	$\frac{\bar{x} - M}{\frac{5}{5}} = \frac{91385 - 73220}{\frac{3920}{\sqrt{100}}} = \frac{46.3265306}{\sqrt{100}}$
5=\$3920	
Conclusion Réject t	

Evidence suggests that California employees with a callege degree do not make the same (on average) than California employees without a college degree.

2-pap percent problem / Indupendent Samples

3. (22 points) Researchers wondered if there was a difference between males and females in regard to some common annoyances. They asked a random sample of males and females, the following question: "Are you annoyed by people who repeatedly check their mobile phones while having an in-person conversation?" Among the 526 males surveyed, 198 responded "Yes". Among the 543 females surveyed, 216 responded "Yes." Does the evidence suggest a higher proportion of females are annoyed by this behavior at the 0.08 significance level? Use the p-value method.

Use the p-value method.	
Popl=All Males	pop 2 = All temales
Q - The percentage of all males	Pg = The percentage of all temaler
that got assaud when a	that get annoyed when a
De stan is constantly the thing	person is constrained while
their mobile phone while	having an in-person conversation
hoving an in-person conversation	a de 2
Somple	Sompi(-
$n_1 = 526 \times 1 = 198 \hat{p}_1 = \frac{\chi_1}{n_1} = \frac{198}{526}$	$n_2 = 593 \times 2 = 016 P_2 = \frac{1}{N_2} = \frac{1}{543}$
$\hat{\rho} = \frac{\times 1 + \times 2}{n_1 + n_2} = \frac{198 + 216}{526 + 543} = \frac{414}{1069}$	$\hat{g} = 1 - \hat{p} = \frac{1069}{1069} - \frac{414}{1069} = \frac{655}{1069}$
Hyp. Test Tegt start	(192) 214
$H_0: P_1 = P_2 = \frac{1}{2} (\hat{r}_1 - \hat{r}_2) - (P_1 - P_2) - (P_1 - P_2)$	(P_2) $(\frac{110}{526} - \frac{1}{543}) = (0)$
$H : P < P_2$	
$JP Q \int \overline{n}, \overline{n} Q$	1069 1069 526 543
Z=-0.7169	8816243
andres of a light	Conclusion Do not reject Ho!
p-volue p-volue	Not enough evidence to say
= p(Z - 0.71688167)	45) that a higher proportion
- 0.2367	OF Females are annoyed
JS p-value	ed: by this behavior
-0,716991674C Z dist 0,23672	0.08? No.
	*

4. (22 points) A doctor says that the standard deviation of the lengths of stay for patients involved in a crash in which the vehicle struck a tree is 6.14 days. A random sample of 30 lengths of stay for patients involved in this type of crash has a standard deviation of 5.8 days. At the $\alpha = 0.05$ level of significance, can you reject the doctor's claim? Use the p-value method.

1-pop J problem

<u>Test stat</u> n:30 5:5.8 Hyp. Test Ho: 0=6.14 days $\chi^{2} = \frac{(n-1)5^{2}}{5^{2}} = \frac{(30-1)(5.8)^{2}}{(6.14)^{2}}$ H1: J = 6.14 2 ay5 J = The standard deviation - 25.877197636 For the lengths of stay For all patients involved in a crash where the vehicle struck on tree Conclusion p-value df=n-1=30-1=29 Do not reject Ho! x > 0.05 p-value p-voint = 2. P(x² < 25.877197636) Not enough Evidence to = 0.7359 o,7359 < 0.05?) doctors claim. IS p-verlue EQ? No ! MANINI MIN 25.877197636 bec. 5< T 2 151. 5.8 26.14

1-pop percentage problem

5. (22 points) In 2015, the proportion of California residents who lived in an apartment was 19.3%. To see if this proportion has dropped since then, 380 California residents were randomly selected and 64 said that they currently live in an apartment. Test the claim at the 0.04 level of significance. Use the p-value method.

Test Synt Hyp. Test n = 380 x = 64 $\hat{p} = \frac{x}{n} = \frac{64}{380}$ Ho: p = 19.3 % H1: P < 19.3 % $Z = \frac{\hat{p} - p}{\int \frac{p e'}{n}} = \frac{64}{380} - 0.193$ (0.193)(0.807)p = The percentage of of all California residents who currently live in an apartment = -1.214058618 p-volue p-volue 2=0.04 = P(Z<-1.214058618) = 0.11236 Is prolue = of? 0.11236 20.04? No. ١ ELUNITY \bigcirc -1.214058618 Do not reject Ho! Conclusion Not enough evidence to say that the percentage afall

California residence who correctly live in an apartment has dropped since 2015. 6. (7 points) What does a the 0.03 mean in a hypothesis test that is performed at the 0.03 significance level.

If you perform the same hypothesis test mony times, each time with a new sample, you will reject the when the is true about 3% of the time.

7. (3 points) What is a type II error?

when you do not reject Ho when Ho is Folse

Some formulas you may need:

$$t = \frac{\overline{x} - \mu}{\frac{s}{\sqrt{n}}} \qquad \qquad df = n - 1$$

$$z = \frac{\hat{p} - p}{\sqrt{\frac{pq}{n}}}$$

$$\chi^2 = \frac{(n-1)s^2}{\sigma^2} \qquad df = n-1$$

$$z = \frac{\hat{p}_1 - \hat{p}_2 - (p_1 - p_2)}{\sqrt{\hat{p}\hat{q}}\sqrt{\frac{1}{n_1} + \frac{1}{n_2}}} \qquad \qquad \hat{p} = \frac{x_1 + x_2}{n_1 + n_2}$$

$$t = \frac{\overline{d} - \mu_d}{\frac{s_d}{\sqrt{n}}} \qquad t = \frac{(\overline{x}_1 - \overline{x}_2) - (\mu_1 - \mu_2)}{\sqrt{\frac{s_1^2}{n_1} + \frac{s_2^2}{n_2}}} \qquad df = \text{smaller of } n_1 - 1 \& n_2 - 1$$

$$F = \frac{s_1^2}{s_2^2} \qquad df_1 = n_1 - 1 \qquad df_2 = n_2 - 1$$

$$s = \sqrt{\frac{\sum (x - \overline{x})^2}{n - 1}} = \sqrt{\frac{\sum x^2 - \frac{(\sum x)^2}{n}}{n - 1}}$$